



INTERNATIONAL  
EDITION

# Data Structures and Algorithm Analysis in Java™

Third Edition

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# Data Structures and Algorithm Analysis in Java

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